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# Generation and Assessment of VMF1-Type Grids Using North-American Numerical Weather Models

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# Overview

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- Use of Numerical Weather Models (NWM) for geodetic purposes
- IERS Conventions
  - Vienna Mapping Functions 1
- Comparison of VMF1 and zenith delays
  - ECMWF, NCEP, CMC-GEM
- Tests using VLBI CONT08
- Conclusions and Future Work

# Numerical Weather Models for Geodesy

- NWM are being used for modeling troposphere delay, atmospheric pressure loading, gravity effects, ....
- Generally, a lack of consistency. Progress being made: <http://ggosatm.hg.tuwien.ac.at/>
- Redundancy concerns

# Troposphere Delay Modelling

According to IERS Conventions (2010):

$$\Delta L = \overbrace{\Delta L_h^z \cdot mf_h(e)}^{\text{Hydrostatic}} + \overbrace{\Delta L_w^z \cdot mf_w(e)}^{\text{Non-hydrostatic}}$$

The diagram illustrates the relationship between Zenith Delays and Mapping Functions in the troposphere delay equation. The equation is  $\Delta L = \Delta L_h^z \cdot mf_h(e) + \Delta L_w^z \cdot mf_w(e)$ . Red brackets above the equation group the terms into 'Hydrostatic' (for  $\Delta L_h^z \cdot mf_h(e)$ ) and 'Non-hydrostatic' (for  $\Delta L_w^z \cdot mf_w(e)$ ). Below the equation, two labels 'Zenith Delays' and 'Mapping Functions' have arrows pointing to the respective terms in the equation. 'Zenith Delays' has arrows pointing to  $\Delta L_h^z$  and  $\Delta L_w^z$ . 'Mapping Functions' has arrows pointing to  $mf_h(e)$  and  $mf_w(e)$ .

# Vienna Mapping Functions 1

- Derived from ECMWF (6 hour basis):

$$mf(\epsilon) = \frac{1 + \frac{a}{1 + \frac{b}{1 + c}}}{\sin \epsilon + \frac{a}{\sin \epsilon + \frac{b}{\sin \epsilon + c}}}$$

- $a$  -- Ray-tracing at fixed elevation angle of 3.3 degrees  
 $b, c$  -- from empirical functions, latitude and day-of-year dependent

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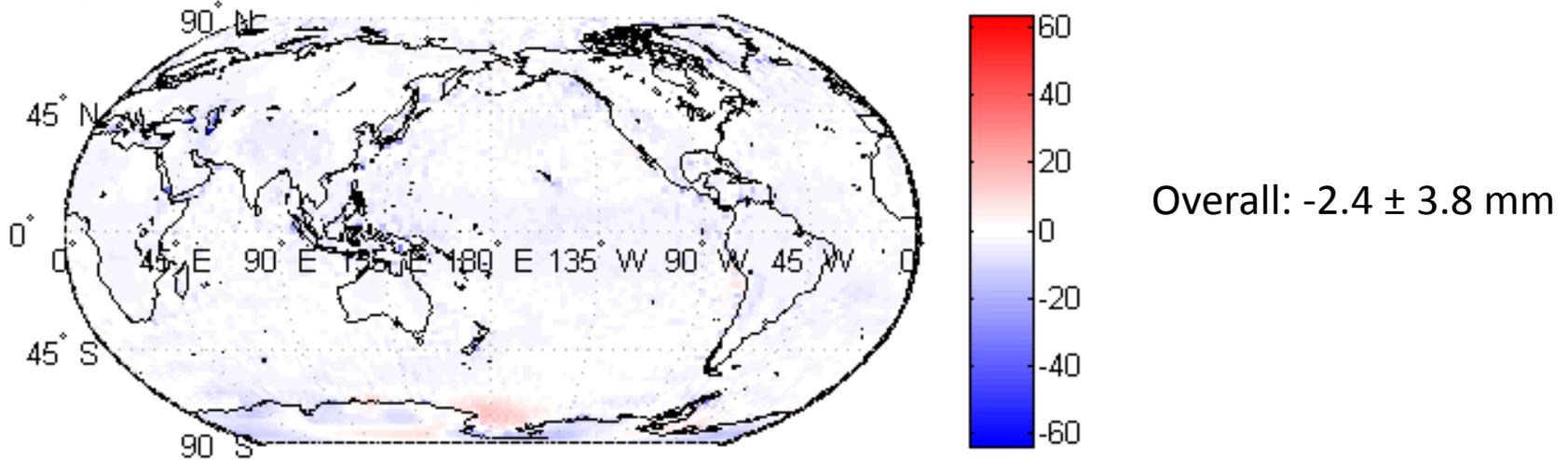
# UNB Realizations of VMF1

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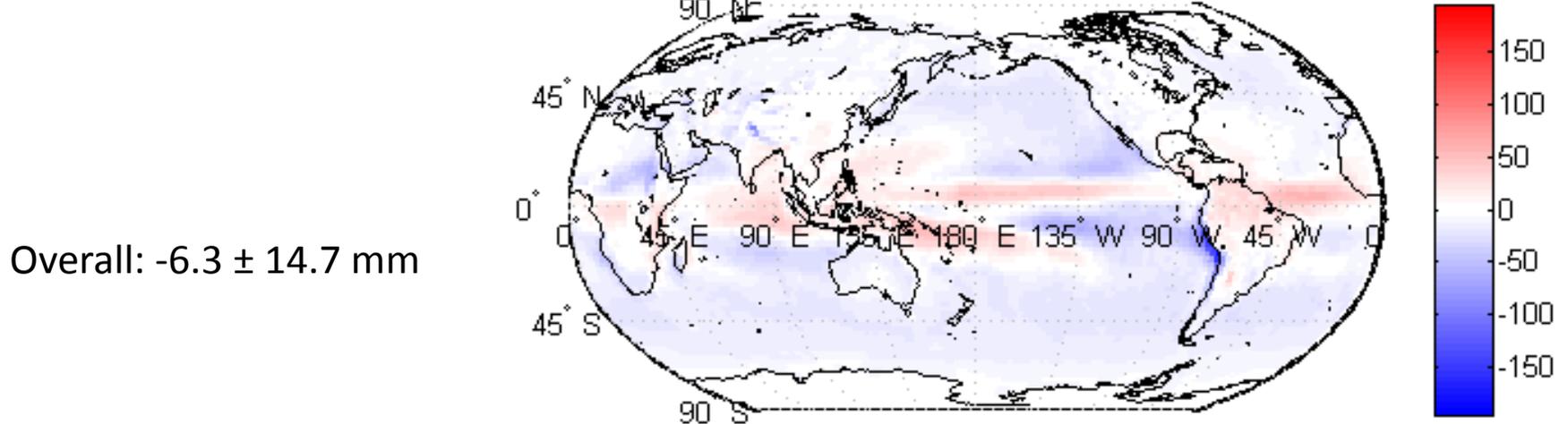
- UNB implementation:
  - NOAA-NCEP Reanalysis (also CMC-GEM)
  - Available on 6 hour basis
  - Only use gridded format (2.0 x 2.5 lat. – long. grid)
    - See <http://ggosatm.hg.tuwien.ac.at/DELAY/readme.txt>
- Independent ray-tracing algorithms
  - Nievinski (2009)

# Zenith Delay Comparison (2010)

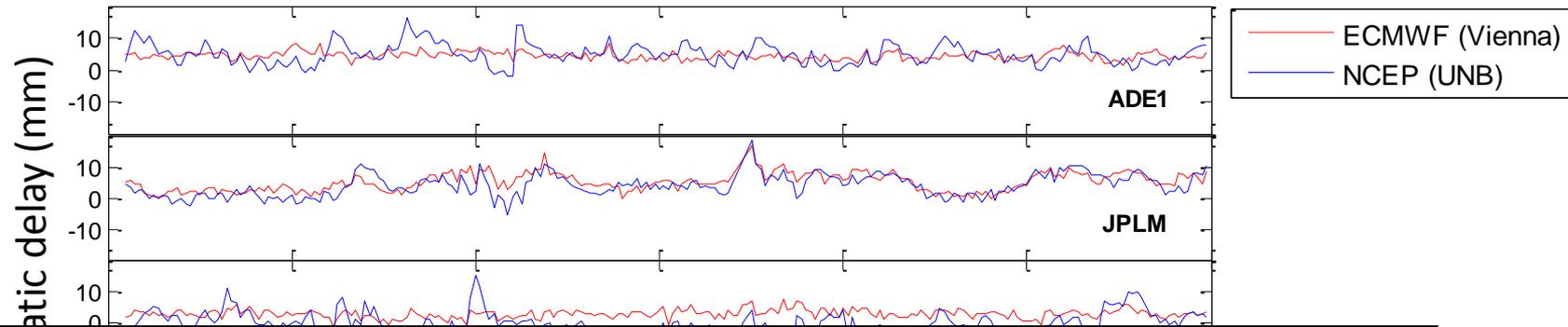
Hydrostatic zenith delays (ECMWF minus NCEP) mm



Non-hydrostatic zenith delays (ECMWF minus NCEP) mm



# Comparison w.r.t. Saastamoinen Delays



## Average statistics over all stations

### Zenith Hydrostatic Delays

### Bias

### Std. Dev.

ECMWF (Vienna)

3.27 mm

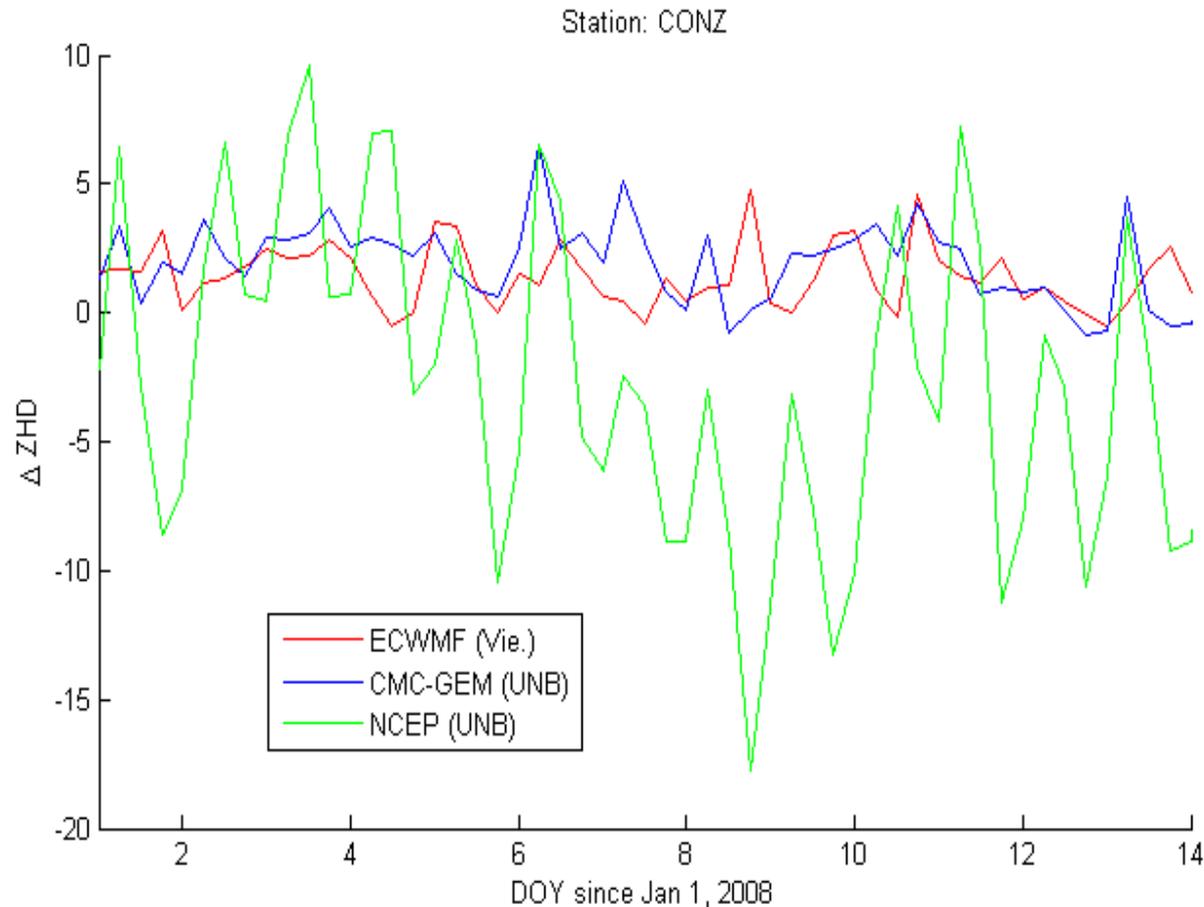
2.18 mm

NCEP (UNB)

1.95 mm

4.22 mm

# Comparison w.r.t Saastamoinen Delays



NCEP ZHD much noisier. Believed to be implementation issue in treatment of NCEP data in our algorithms

# — Comparison of Mapping Function Errors —

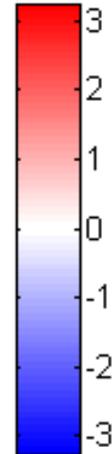
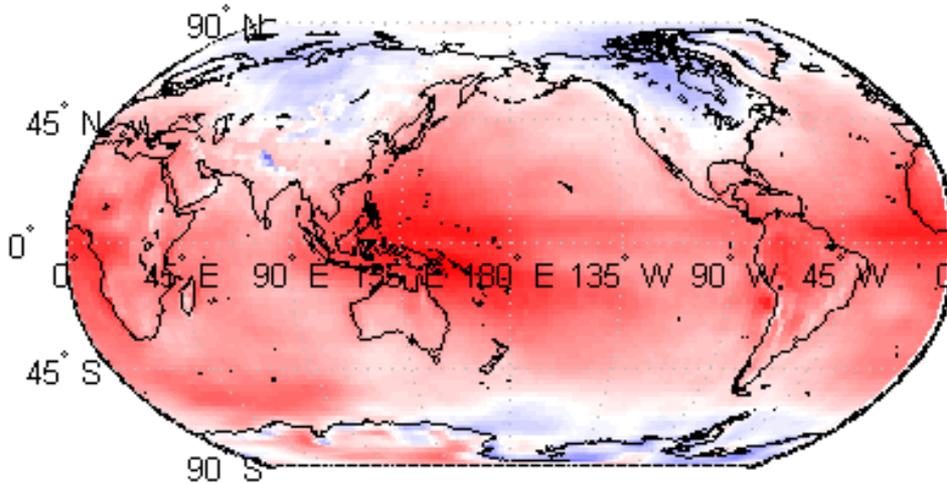
- Use rule of thumb (MacMillan and Ma, 1994; Boehm et al., 2008):

***Bias in station height is  
approximately equal to  
1/5 bias in slant delay at 5 degrees elevation  
angle***

# Difference in Station Height due to Mapping Functions

Hydrostatic (ECMWF minus NCEP)

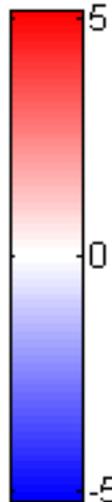
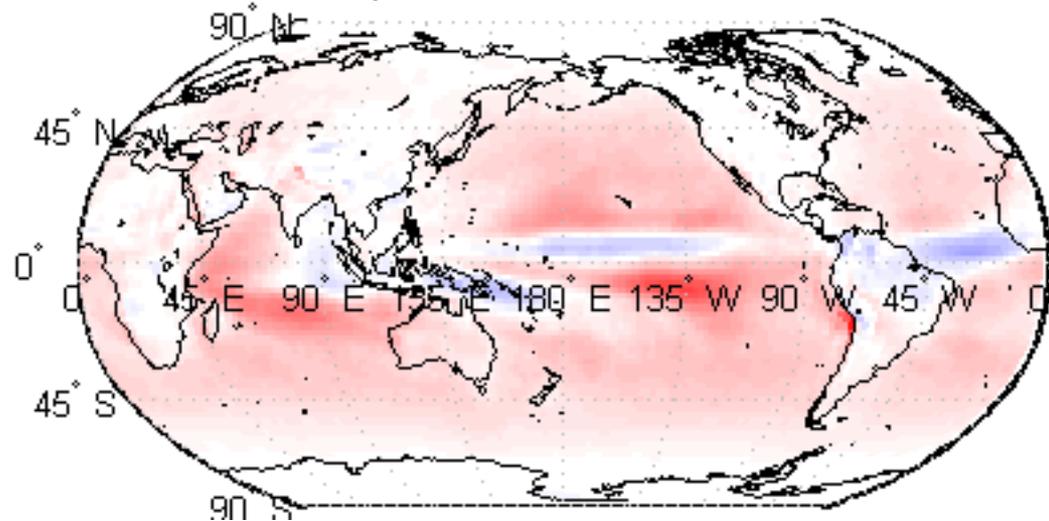
mm



Overall:  $0.79 \pm 0.89$  mm

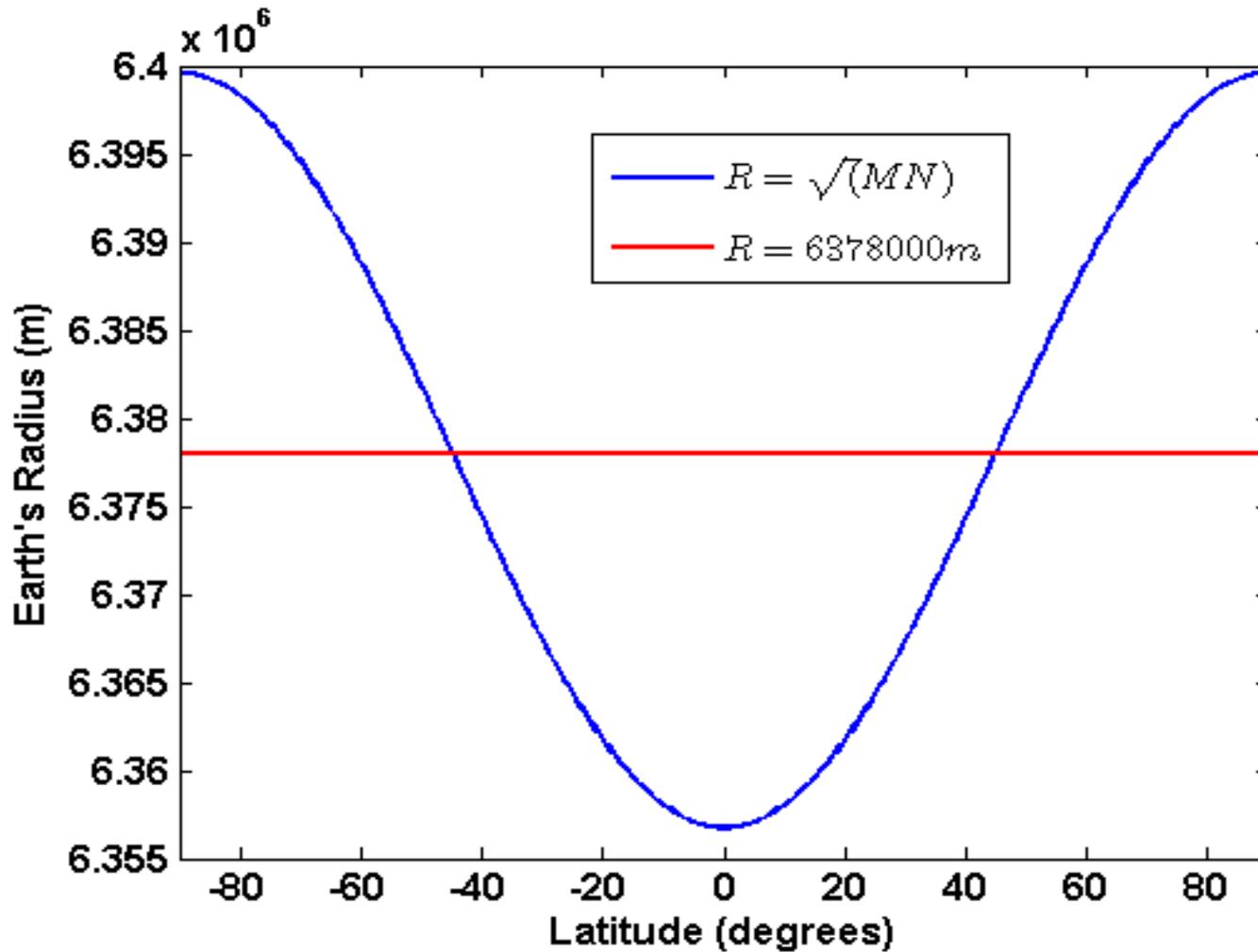
Non-Hydrostatic (ECMWF minus NCEP)

mm



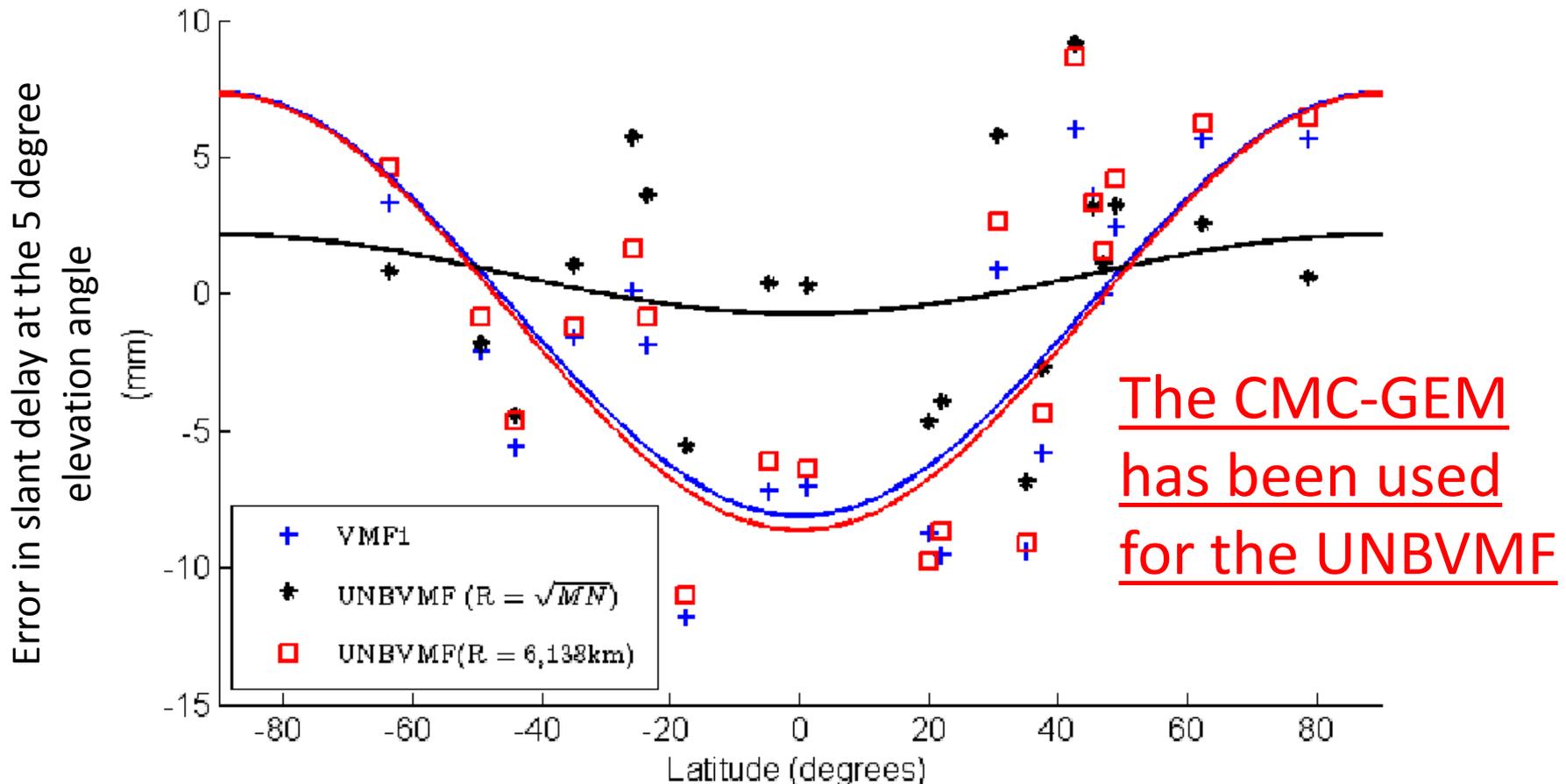
Overall:  $0.4 \pm 0.58$  mm

# Effect of Earth's Radius on Slant Hyd. Delay



# Comparison to 3D ray-tracing

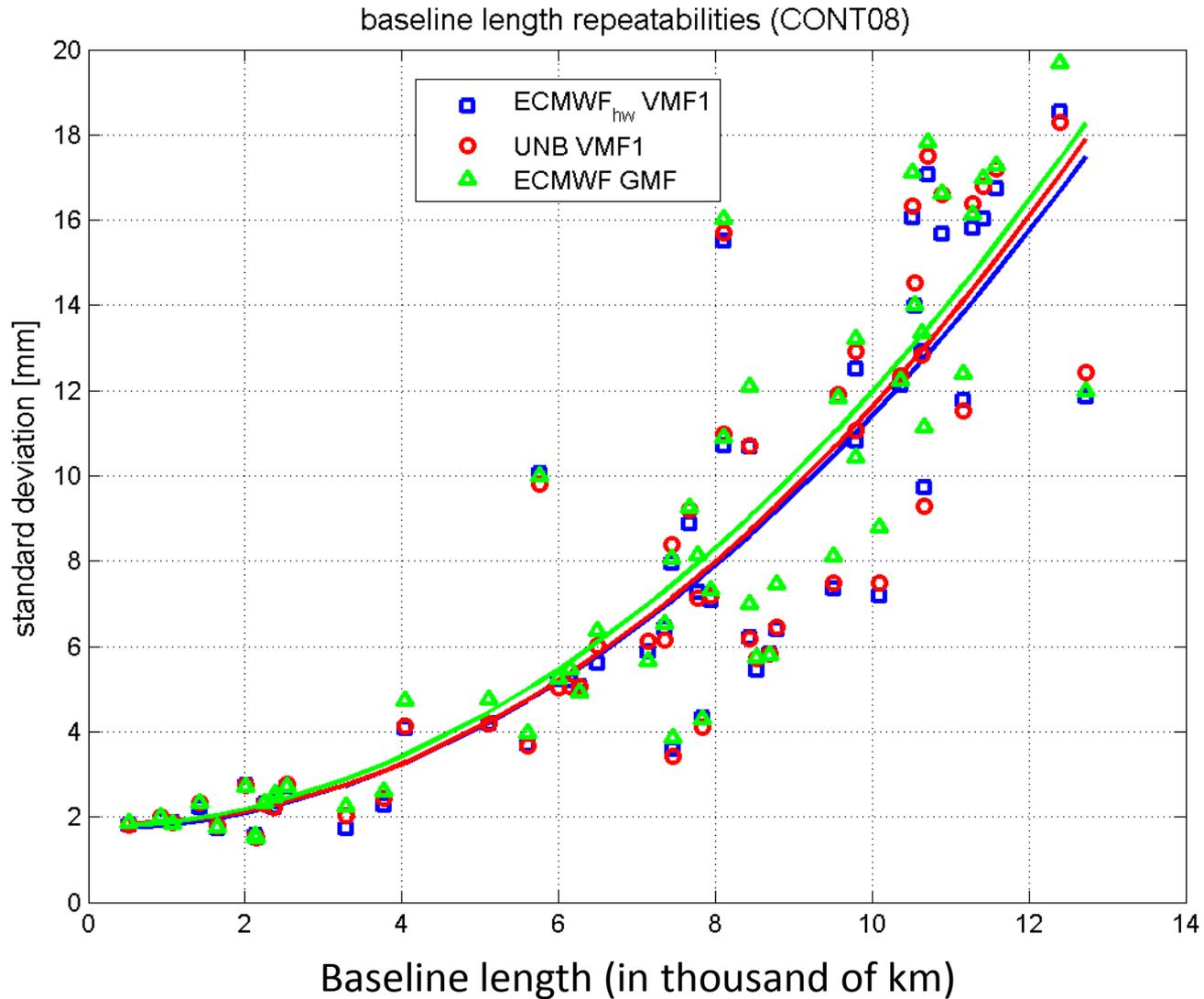
Three dimensional ray-tracing uses ellipsoidal coordinates



Systematic effect of  $\pm 2\text{mm}$  error in station height

# VLBI Results – CONT08

CONT08 ...  
see JOGE  
Vol. 85,  
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# Conclusion

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1. NWM will continue to improve. As they do, they will become more useful for geodetic purposes.
2. We have been generating VMF1-type grids using NCEP and CMC-GEM models at UNB.
3. Addresses consistency and redundancy issues.
4. Test results:
  1. Zenith delays (ECMWF – NCEP):
    - Hydrostatic:  $-2.4 \pm 3.8$  mm
    - Non-hydrostatic:  $-6.3 \pm 14.7$  mm
  2. Comparison to Saataainen:
    - NCEP: 2 mm (bias); 4 mm (st. Dev.)
    - NCEP “noisier” than GEM

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# Conclusion

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## 5. Test results (cont.):

### 3. Difference in Station Height (ECMWF – NCEP):

- Hydrostatic:  $0.8 \pm 0.9$  mm
- Non-hydrostatic:  $-0.4 \pm 0.6$  mm

### 1. Different radius of curvature:

1.  $\pm 2$  mm difference

### 2. Impact on baseline repeatability (VLBI CONT08):

1. VMF1 and UNB-VMF1 closer together than GMF
2. GMF  $\rightarrow$  higher values

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# Future Work

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- Tests ... More tests!
- Comparisons in the position domain
  - GPS campaigns, effect on mean station position
- Provision of UNB-VMF1 to public
  - Similar to current service
  - Act as a backup or alternative for users.

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# Acknowledgements

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